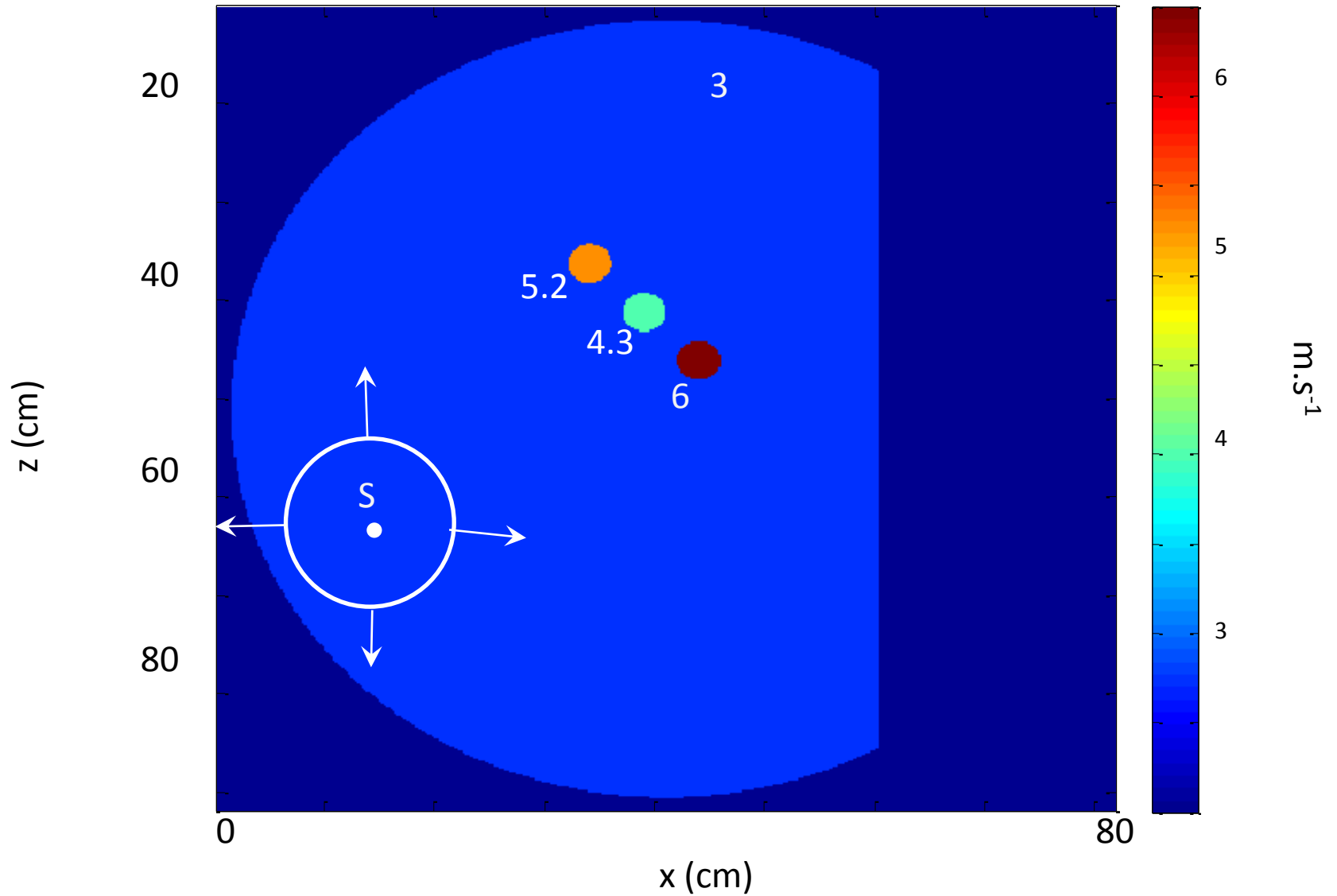


Élastographie et retournement temporel : une tomographie acoustique passive d'ondes de cisaillement dans le corps humain

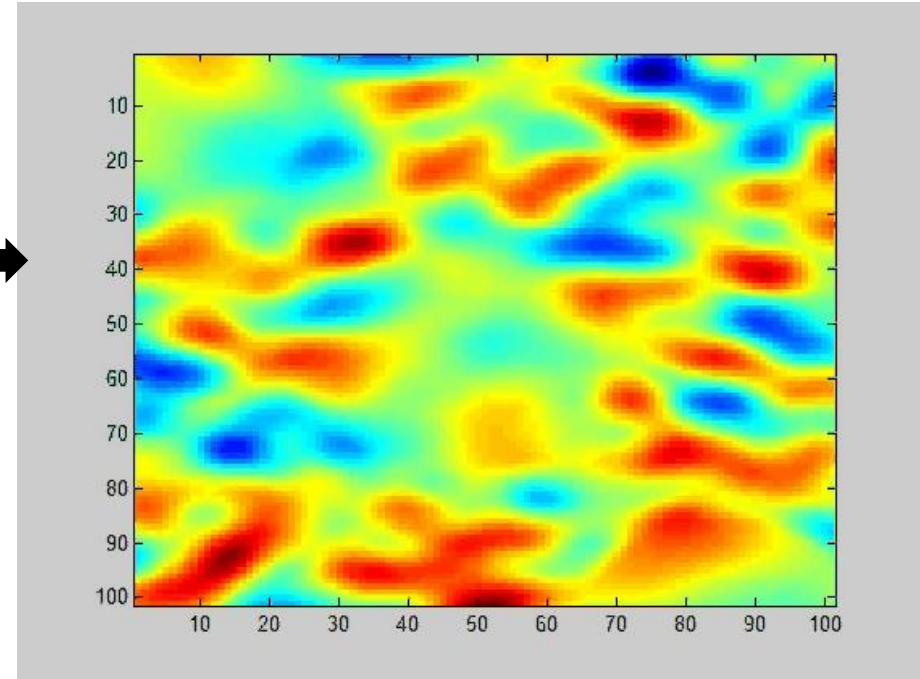
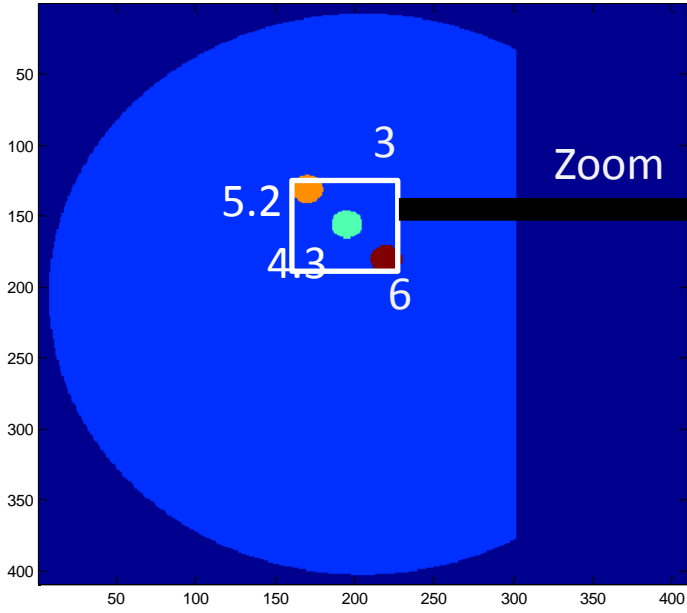
S.Catheline, R.Souchon, A. Hoang-Dinh and J-Y Chapelon

INSERM U1032, LabTAU, University of Lyon

The diffuse field approach: finite difference simulation



The diffuse field approach



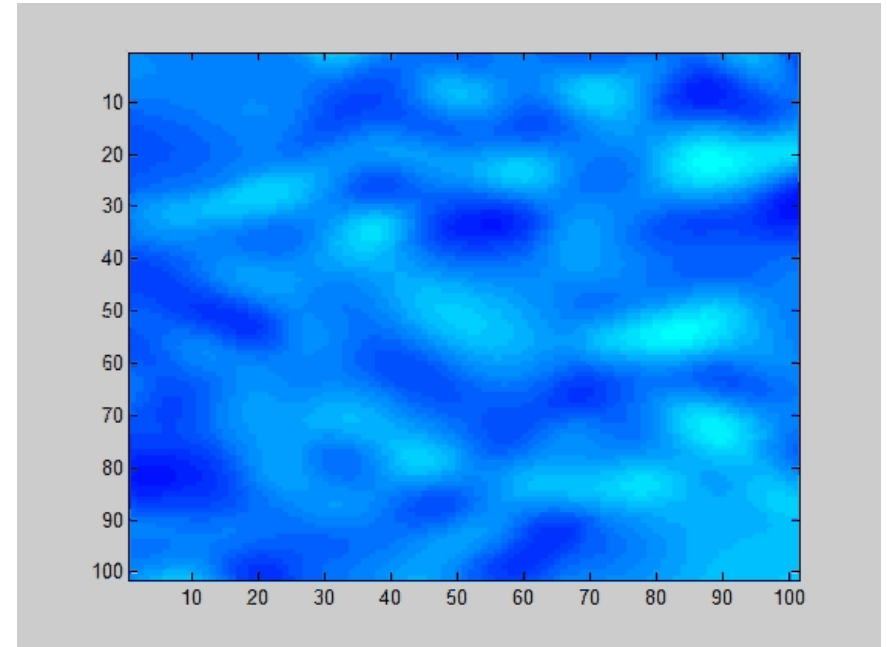
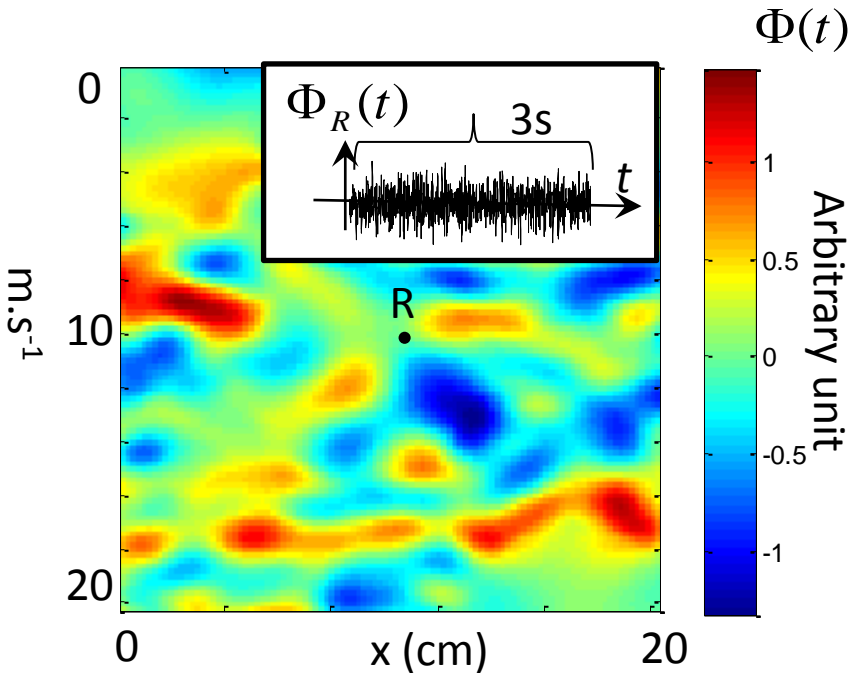
Time reversal

Key for speed extraction=TR

TR=spatio-temporal correlation

$$\Delta\Phi - \frac{1}{c^2} \frac{\partial^2\Phi}{\partial t^2} = 0$$

$$\rightarrow \psi^{RT} = \Phi(\vec{r}, t) \otimes \Phi(\vec{r}_0 - t) = \Phi \Phi^*$$



S.Catheline, N. Benech, X. Brum, and C. Negreira, *Phys.Rev.Letter.* **100**, 064301 (2008).

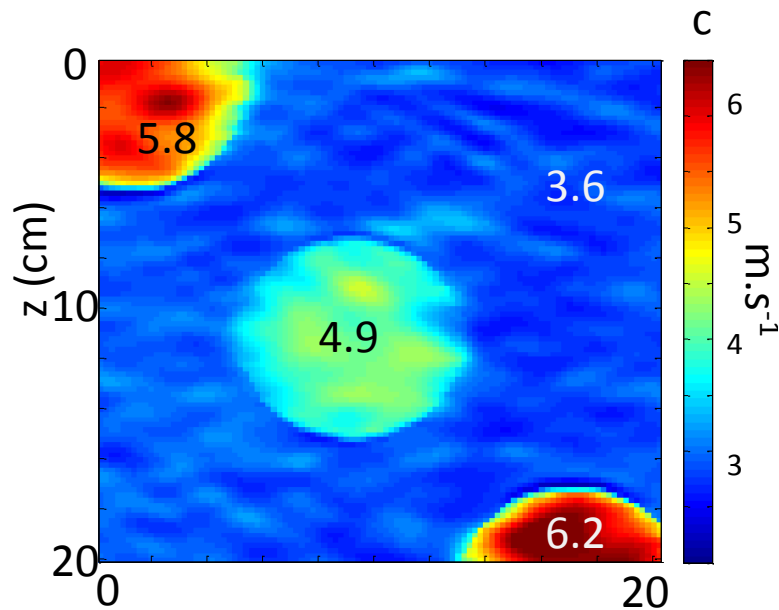
T.Gallot, S. Catheline, P. Roux, J. Brum, N. Benech, C. Negreira, *IEEE UFFC*, vol.58,6,p.1122 (2011)

Generalised time reversal fields

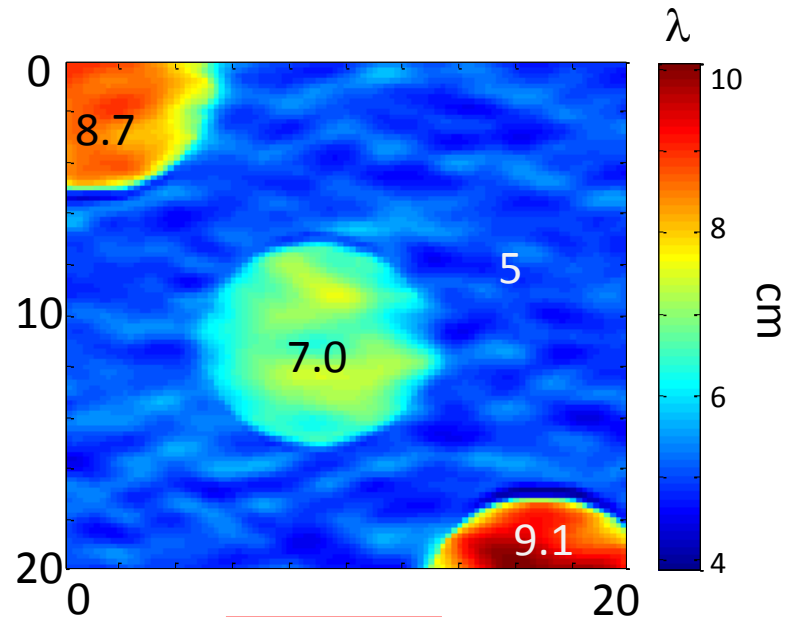
$$\Delta\Phi - \frac{1}{c^2} \frac{\partial^2 \Phi}{\partial t^2} = 0 \quad \rightarrow \quad \psi^{RT} = \Phi(\vec{r}, t) \otimes \Phi(\vec{r}_0 - t) = \Phi \Phi^*$$

$$\varepsilon_z = \frac{\partial \Phi}{\partial z} \quad \rightarrow \quad \Delta \varepsilon_z - \frac{1}{c^2} \frac{\partial^2 \varepsilon_z}{\partial t^2} = 0 \quad \rightarrow \quad \xi^{RT} = \varepsilon_z \varepsilon_z^* \quad \xrightarrow{\text{Plane wave}} \quad \xi^{RT} \approx -k^2 \psi^{RT}$$

$$v = \frac{\partial \Phi}{\partial t} \quad \rightarrow \quad \Delta v - \frac{1}{c^2} \frac{\partial^2 v}{\partial t^2} = 0 \quad \rightarrow \quad V^{RT} = v v^* \quad \rightarrow \quad V^{RT} \approx -\omega^2 \psi^{RT}$$

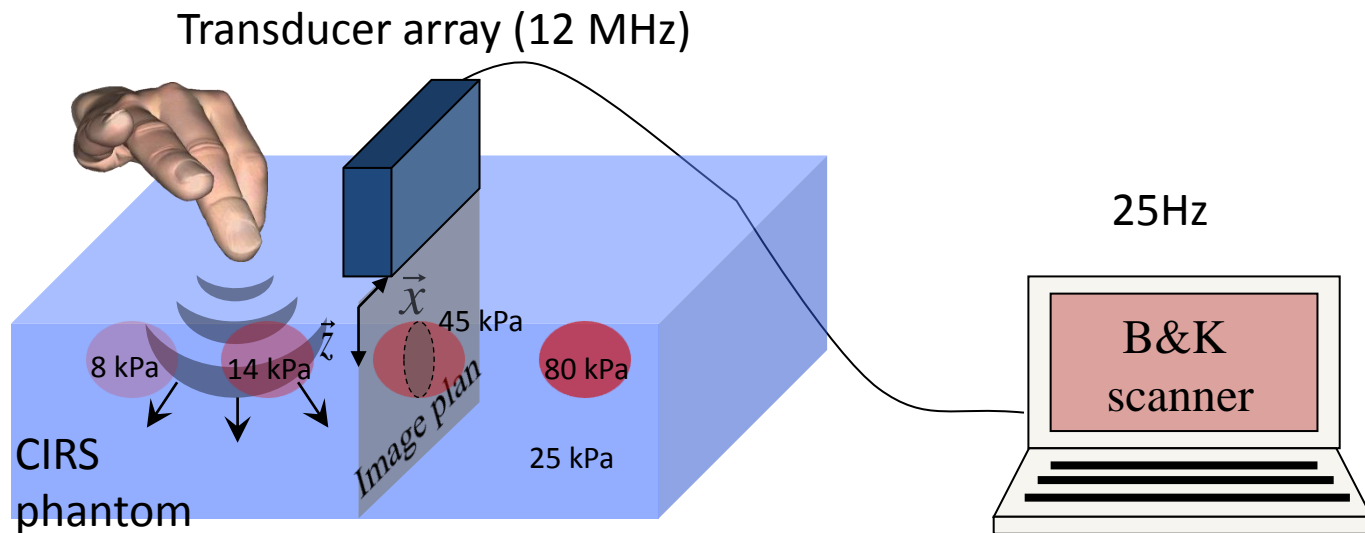


$$c = \frac{\omega}{\text{Re}(k)} = \sqrt{\frac{V^{RT}}{\xi^{RT}}}$$

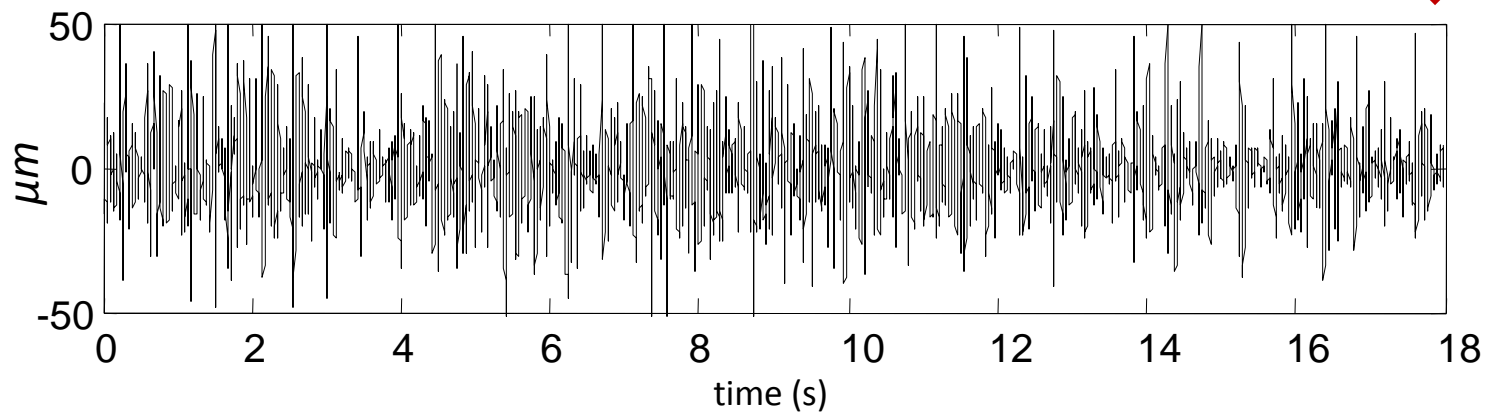


$$k = \sqrt{\frac{\xi^{RT}}{\psi^{RT}}}$$

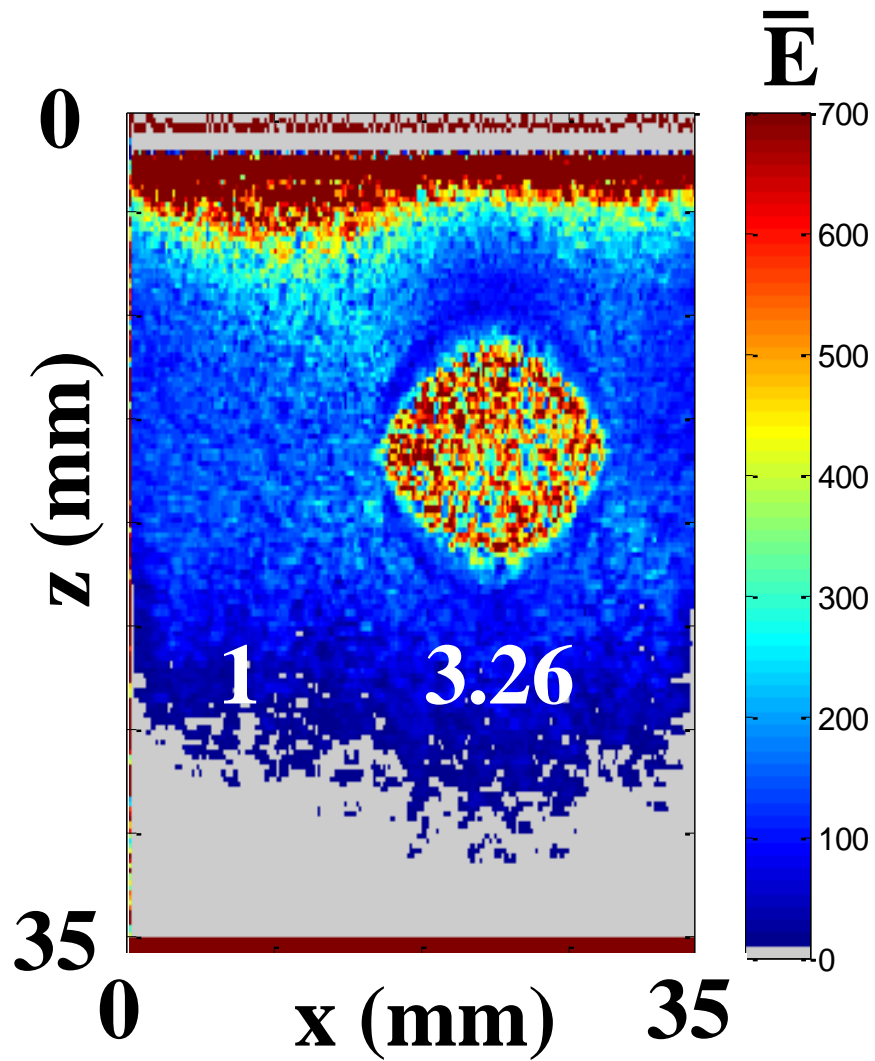
Phantom experiment



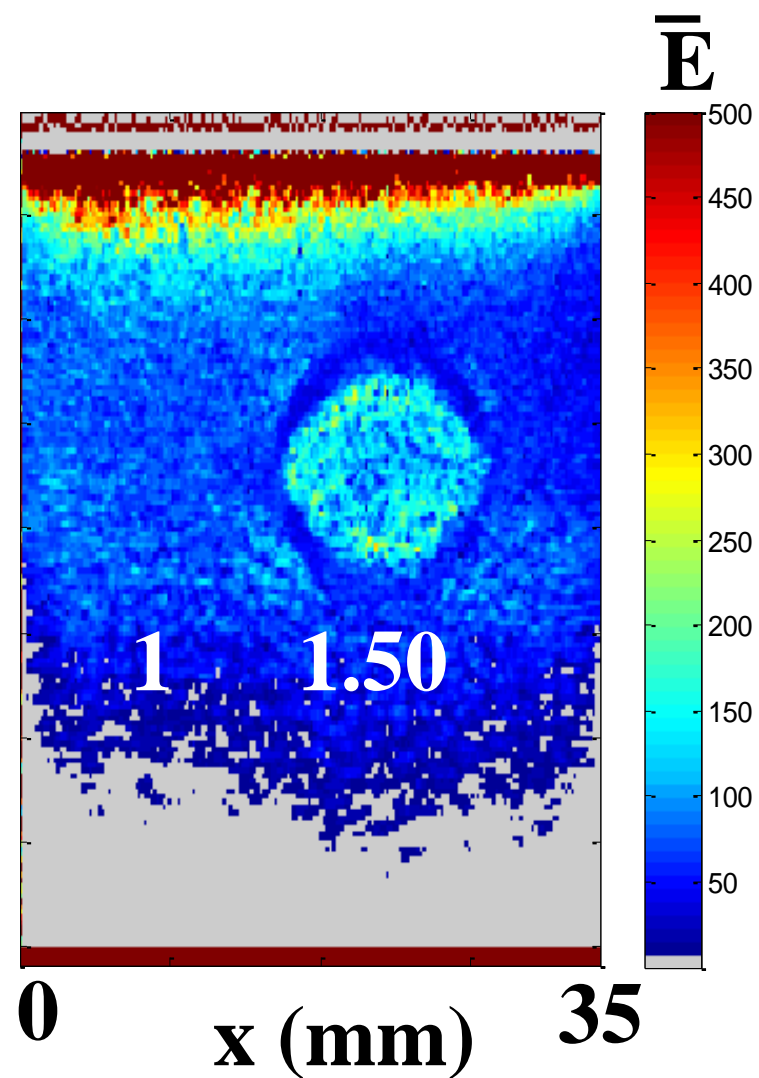
$$\Psi_z(x,z;t)$$



Phantom experiment

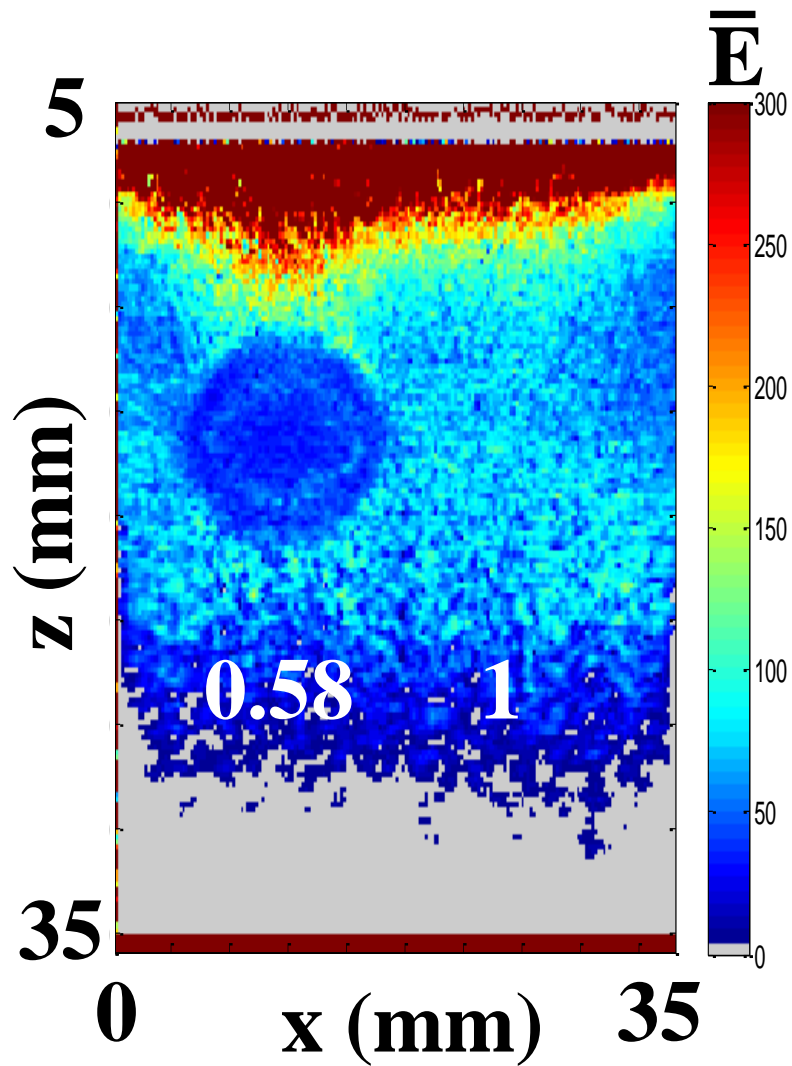


$$\frac{80kPa}{25kPa} = 3.20$$

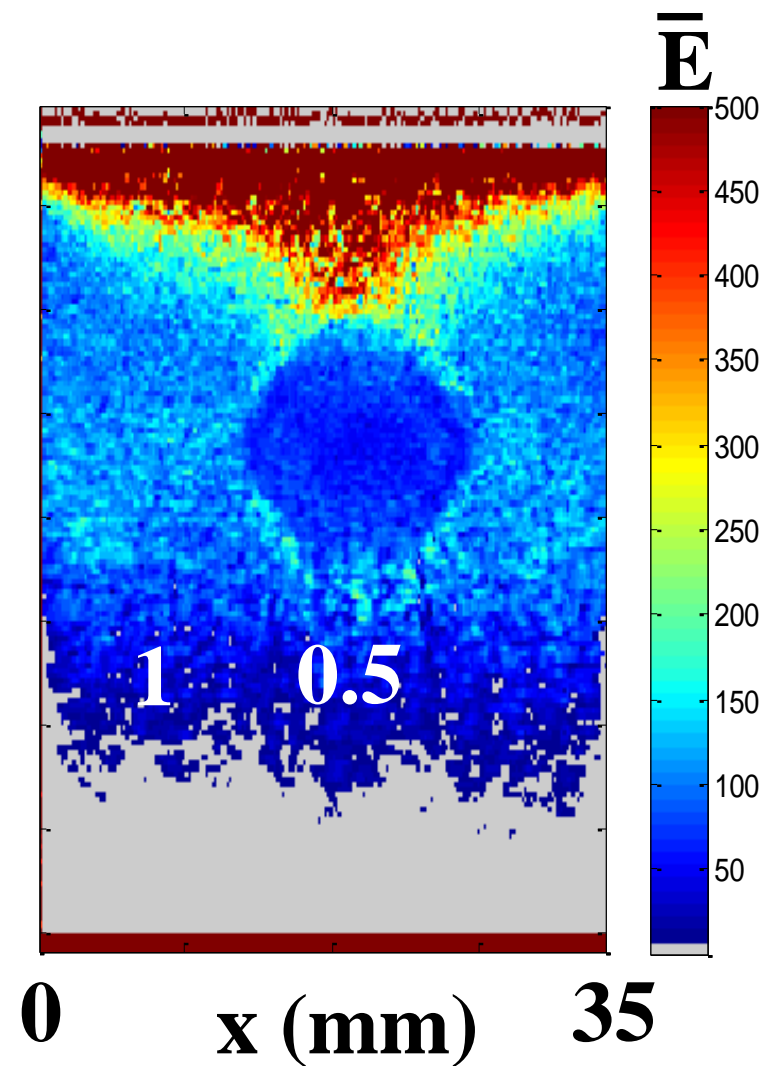


$$\frac{45kPa}{25kPa} = 1.80$$

Phantom experiment



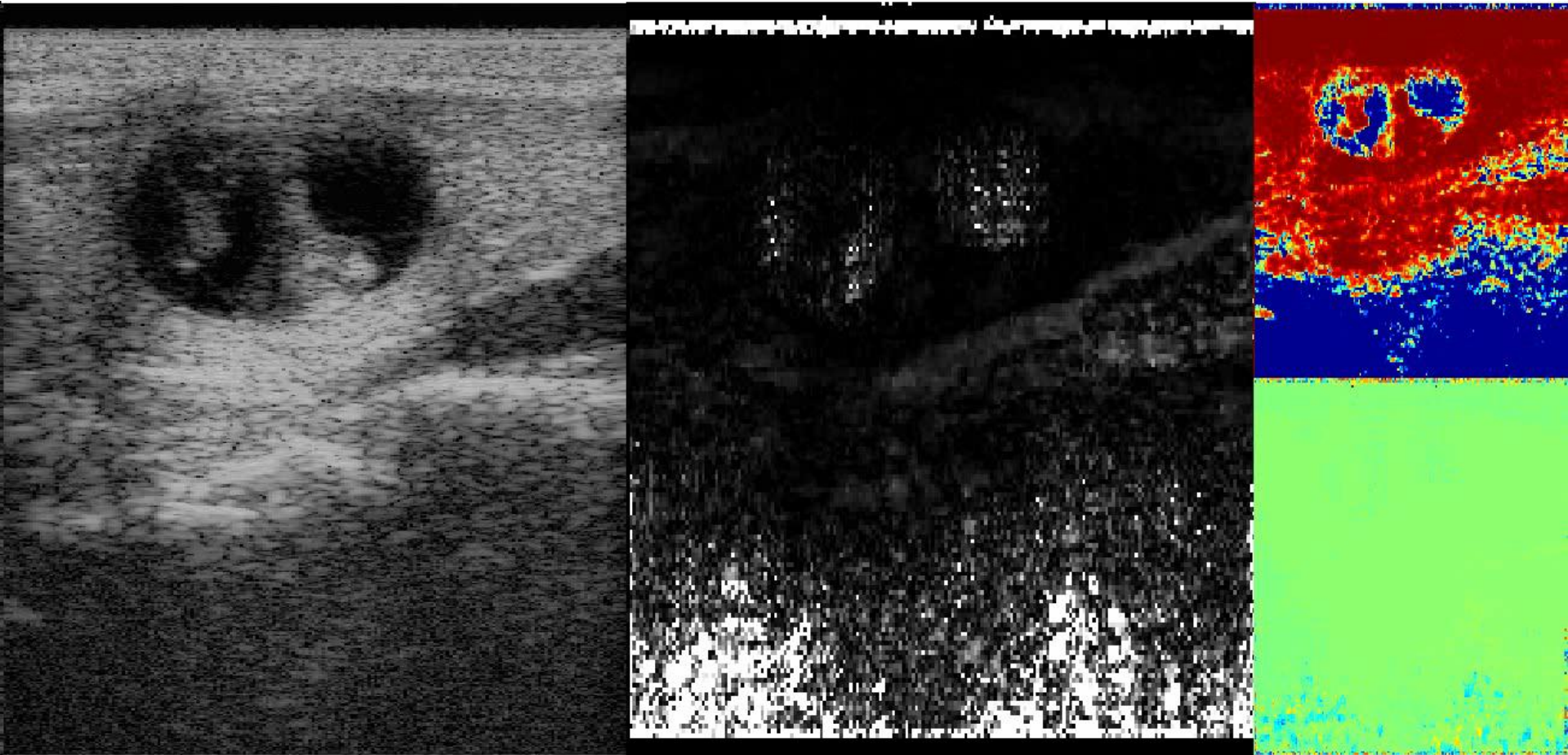
$$\frac{14kPa}{25kPa} = 0.56$$



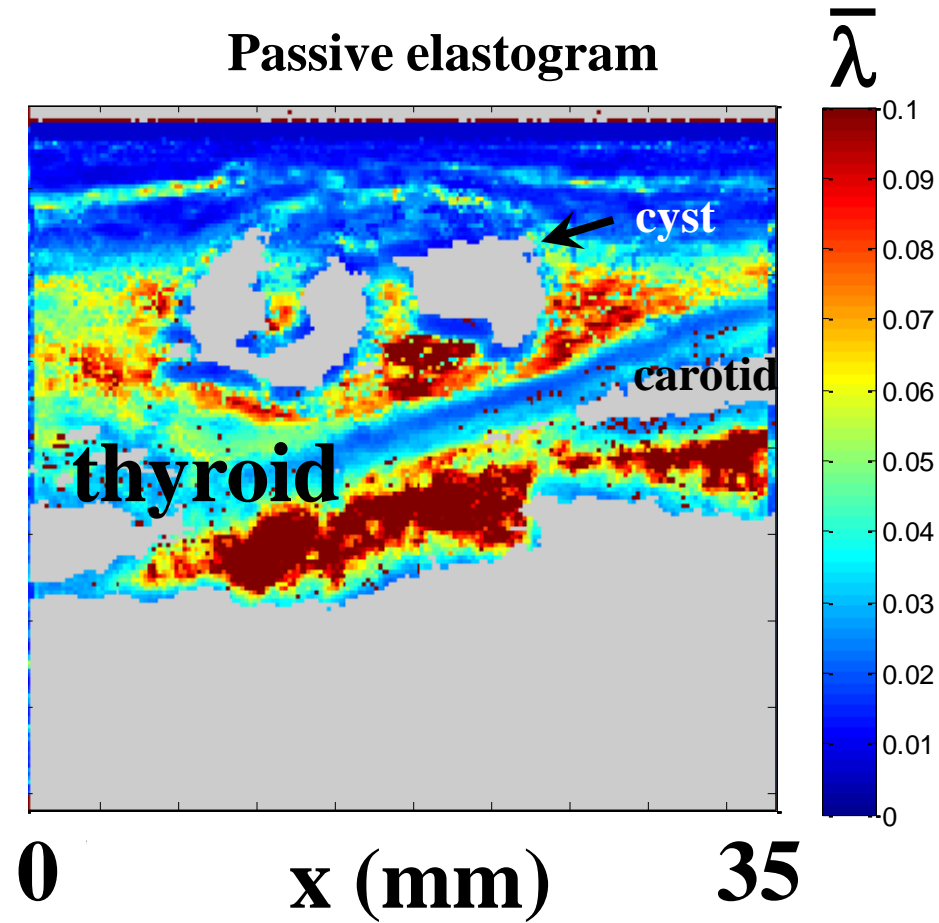
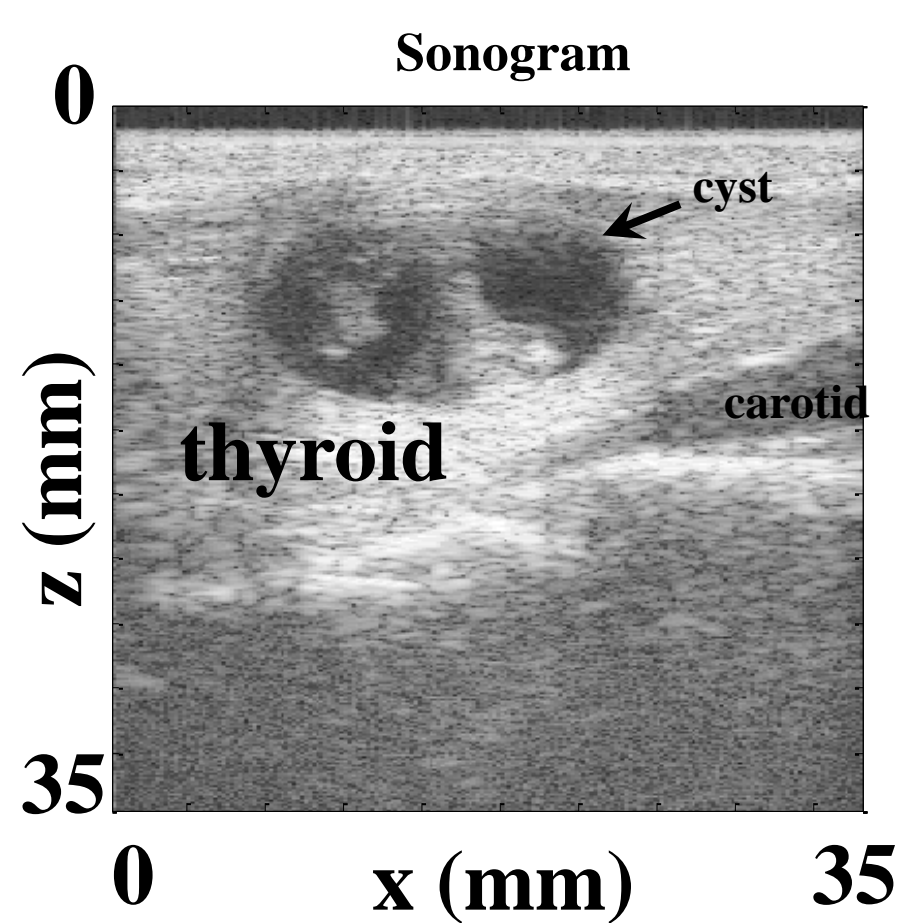
$$\frac{8kPa}{25kPa} = 0.32$$

Preliminary *in-vivo* experiment



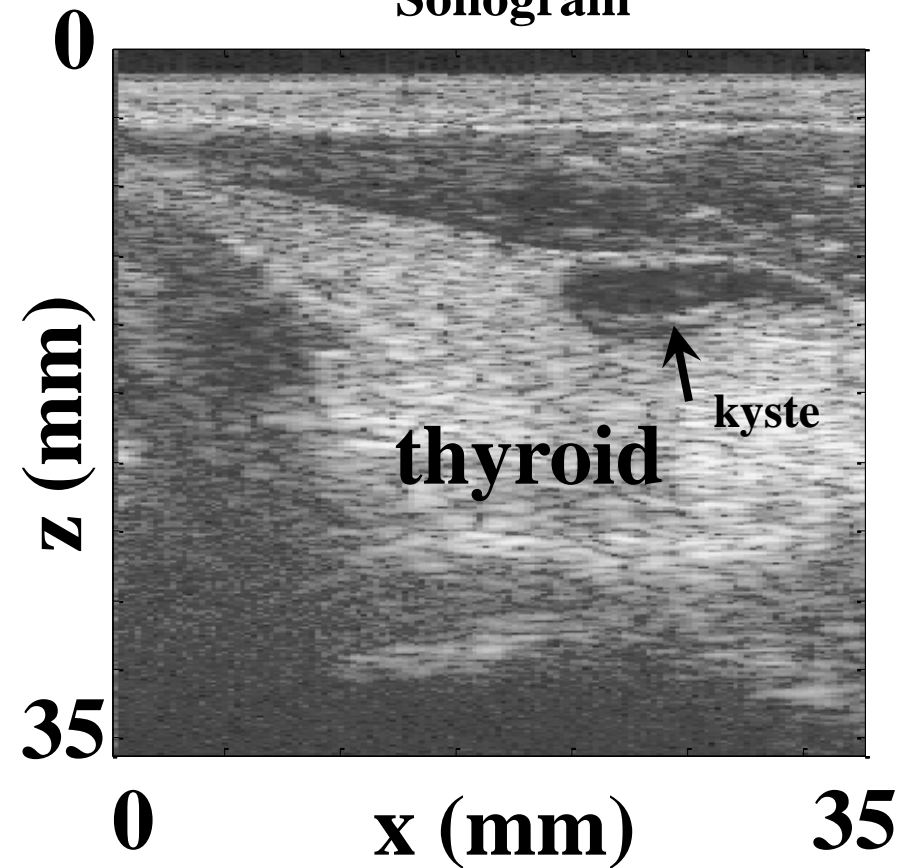


800 images @ 25Hz

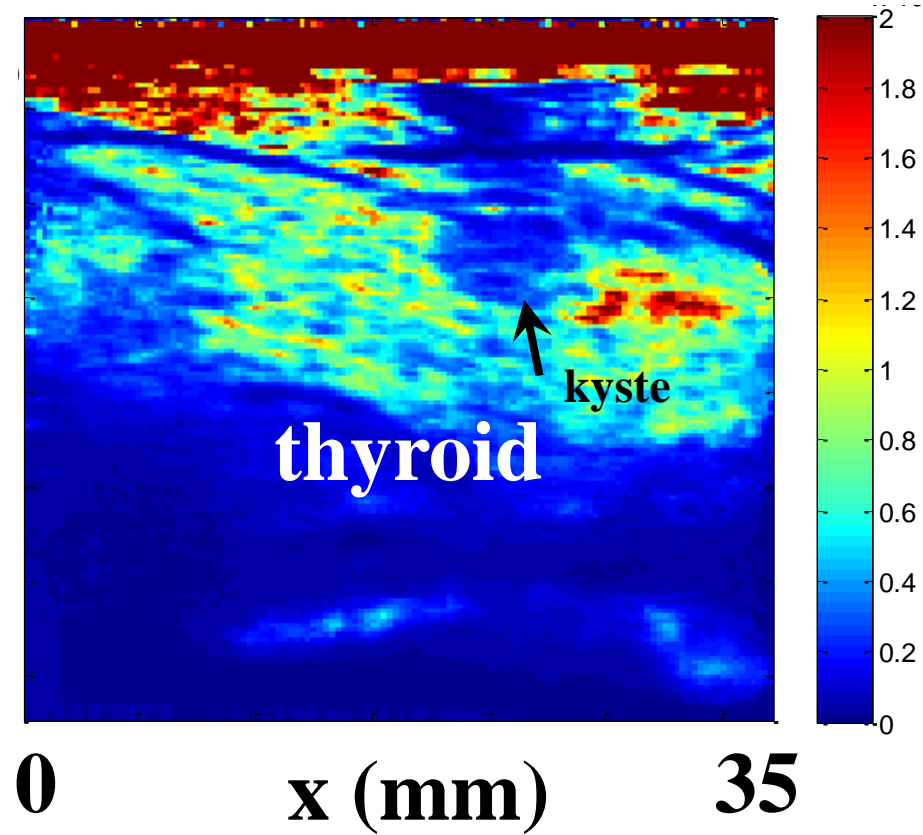


$$k = \sqrt{\frac{\xi^{RT}}{\psi^{RT}}}$$

Sonogram



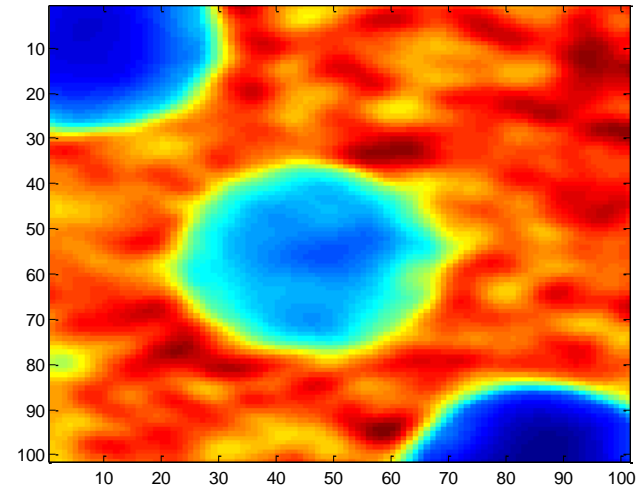
Dynamic elastogram



Equipartition-Green's function

Equipartition of diffuse field: $\psi^{RT} \propto \frac{V}{\lambda^3}$

Green's function
with $G^- = \frac{1}{c^3} \frac{e^{-ikx}}{x}$ $\psi^{RT} = G^- - G^+$



a)



